

CONTINUOUS INTERNAL EVALUATION- 3

Dept: BS	Sem / Div: III/A & B	Sub: Transform Calculus, Fourier series and Numerical Techniques	S Code:18MAT31
Date: 15/02/2021	Time: 9:30-11:00 am	Max Marks: 50	Elective: N
Note: Answer any 2 full questions, choosing one full question from each part.			

Q N	Questions	Marks	RBT	COs
--------	-----------	-------	-----	-----

PART A

1 a	Using Runge – Kutta method of fourth order solve $\frac{dy}{dx} = x + y$, $y(0.4) = 1$ at $x = 0.5$ correct to four decimal places.	8	L2	CO4
b	If $\frac{dy}{dx} = 2e^x - y$, $y(0) = 2$, $y(0.1) = 2.010$, $y(0.2) = 2.040$, $y(0.3) = 2.090$ find $y(0.4)$ corrected to 4 decimal places by using Milne's predictor-corrector method (Use corrector formula twice)	8	L2	CO4
c	Given that $\frac{dy}{dx} = (1+y)x^2$ and $y(1) = 1$, $y(1.1) = 1.233$, $y(1.2) = 1.548$, $y(1.3) = 1.979$ determine $y(1.4)$ by Adams-Bash forth method.	9	L2	CO4

OR

2 a	Apply Runge – Kutta fourth order method to find an approximate value of y when $x = 0.2$ given that $\frac{dy}{dx} = x + y$ and $y = 1$ when $x = 0$.	8	L2	CO4
b	Given that $\frac{dy}{dx} = x^2 + y^2$ and $y(0) = 1$, $y(0.1) = 1.245$, $y(0.2) = 1.6043$, $y(0.3) = 2.1235$, determine $y(0.4)$ by Adams-Bash forth method.	8	L2	CO4
c	Using Milne's predictor-corrector method find y when $x = 0.8$, given $\frac{dy}{dx} = x - y^2$ given $y(0) = 0$, $y(0.2) = 0.02$, $y(0.4) = 0.0795$, $y(0.6) = 0.1762$. Apply corrector formula twice.	9	L2	CO4

PART B

3 a	Using Runge-Kutta method solve $\frac{d^2y}{dx^2} = x \left(\frac{dy}{dx}\right)^2 - y^2$ at $x = 0.2$ with $x_0 = 0$, $y_0 = 1$, $z_0 = 0$, take $h = 0.2$	8	L3	CO4
b	Derive Euler's equation in the standard form viz, $\frac{\partial f}{\partial y} - \frac{d}{dx} \left(\frac{\partial f}{\partial y'} \right) = 0$	8	L3	CO5
c	Prove that the Geodesics on a plane are straight lines.	9	L3	CO5

OR

4 a	Use Milne's method to compute $y(0.8)$ given that $\frac{d^2y}{dx^2} = 1 - 2y \frac{dy}{dx}$ and the following table of initial values.	8	L3	CO4															
<table border="1"> <tr> <td>x</td> <td>0</td> <td>0.2</td> <td>0.4</td> <td>0.6</td> </tr> <tr> <td>y</td> <td>0</td> <td>0.02</td> <td>0.0795</td> <td>0.1762</td> </tr> <tr> <td>z = dy/dx</td> <td>0</td> <td>0.1996</td> <td>0.3937</td> <td>0.5689</td> </tr> </table>					x	0	0.2	0.4	0.6	y	0	0.02	0.0795	0.1762	z = dy/dx	0	0.1996	0.3937	0.5689
x	0	0.2	0.4	0.6															
y	0	0.02	0.0795	0.1762															
z = dy/dx	0	0.1996	0.3937	0.5689															

CONTINUOUS INTERNAL EVALUATION- 3

b	Find the curve on which the functional $\int_0^1 [y^2 + x^2 y'] dx$ with $y(0)=0, y(1)=1$ can be extremized.	8	L3	CO5
c	A heavy cable hangs freely under gravity between two fixed points. Show that the shape of the cable is a catenary.	9	L3	CO5

PART A

CO4	L3	8	Using Runge-Kutta method of fourth order solve $\frac{dy}{dx} = x + y, y(0.4) = 1$ at $x=0.5$ correct to four decimal places.
CO4	L3	8	Use the Runge-Kutta method of fourth order to solve $\frac{dy}{dx} = 2x - y, y(0) = 2, y(0.1) = 2.010, y(0.2) = 2.040, y(0.3) = 2.090$ find $y(0.4)$ correct to 3 decimal places by using Milne's predictor-corrector method (Use corrector formula twice).
CO4	L3	9	Given that $\frac{dy}{dx} = 1 + y^2$ and $y(1) = 1, y(1.1) = 1.233, y(1.2) = 1.518, y(1.3) = 1.979$ determine $y(1.4)$ by Adams-Bashforth method.
OR			
CO4	L3	8	Apply Runge-Kutta fourth order method to find an approximate value of y when $x = 0.2$ given that $\frac{dy}{dx} = x + y$ and $y=1$ when $x=0$.
CO4	L3	8	Given that $\frac{dy}{dx} = x^2 + y^2$ and $y(0) = 1, y(0.1) = 1.242, y(0.2) = 1.6043, y(0.3) = 2.1325$ determine $y(0.4)$ by Adams-Bashforth method.
CO4	L3	9	Using Milne's predictor-corrector method find y when $x = 0.8$ given $\frac{dy}{dx} = x - y$ given $y(0) = 0, y(0.2) = 0.02, y(0.4) = 0.0792, y(0.6) = 0.1762$. Apply corrector formula twice.
PART B			
CO4	L3	8	Using Runge-Kutta method solve $\frac{dy}{dx} = x \left(\frac{dy}{dx} - y \right) - y^2$ at $x=0.2$ with $x_0=0, y_0=1, x_1=0.2$ take $h=0.2$.
CO3	L3	8	Derive Euler's equation in the standard form.
CO3	L3	9	Prove that the Geodesics on a plane are straight lines.
OR			
CO4	L3	8	Use Milne's method to compute $y(0.8)$ given that $\frac{dy}{dx} = 1 - 2y^2$ and $y(0) = 0, y(0.2) = 0.192, y(0.4) = 0.3937, y(0.6) = 0.5889$.